## CHAPTER 1: SUPPLEMENTARY PROBLEMS <br> MEASUREMENTS

S1-1. Write the following quantities in exponential notation, with one digit to the left of the decimal point (e.g., $17 \mathrm{fC}=1.7 \times 10^{-14} \mathrm{C}$ ):
(a) 2 TJ
(c) 37 Mm
(e) 842 pF
(b) 37 mm
(d) 4 dK
(f) 18.4 kPa

S1-2. Express the following quantities with abbreviations for units and prefixes from Tables 1-1 through 1-3:
(a) $8 \times 10^{-5}$ moles
(c) $4 \times 10^{-7}$ liters
(e) $1.8 \times 10^{14}$ hertz
(b) $1 \times 10^{10}$ watts
(d) $3 \times 10^{-2}$ meters
(f) $537 \times 10^{10}$ ohms

S1-3. The lowest temperature attained in the laboratory in 1990 was 800 pK (for the nuclei of silver atoms). Solid ${ }^{3} \mathrm{He}$ has been cooled to $43 \mu \mathrm{~K}$. Express the quotient $800 \mathrm{pK} / 43 \mu \mathrm{~K}$ in exponential notation (i.e. $a \times 10^{b}$ ).

S1-4. Use Table 1-4 to confirm that there are 760 torr in 1 atm .
S1-5. If 0.250 L of aqueous solution with a density of $1.00 \mathrm{~g} / \mathrm{mL}$ contins $13.7 \mu \mathrm{~g}$ of pesticide, express the concentration of pesticide in (a) ppm and (b) ppb.

S1-6. High purity water required in the semiconductor industry is purified by a process called deionization in which most cations and anions are replaced by $\mathrm{H}^{+}$and $\mathrm{OH}^{-}$, respectively. (The product of $\mathrm{H}^{+}+\mathrm{OH}^{-}$is just $\mathrm{H}_{2} \mathrm{O}$.) The average concentrations of some residual cations and anions left after deionization in one high purity industrial water line are shown below:

| $\mathrm{Na}^{+}$ | $154 \mathrm{ng} / \mathrm{L}$ | $\mathrm{Cl}^{-}$ | $172 \mathrm{ng} / \mathrm{L}$ |
| :--- | ---: | :--- | ---: |
| $\mathrm{NH}_{4}^{+}$ | $58 \mathrm{ng} / \mathrm{L}$ | $\mathrm{Br}^{-}$ | $<10 \mathrm{ng} / \mathrm{L}$ |
| $\mathrm{K}^{+}$ | $63 \mathrm{ng} / \mathrm{L}$ | $\mathrm{NO}_{3}^{-}$ | $26 \mathrm{ng} / \mathrm{L}$ |
| $\mathrm{Mg}^{2+}$ | $73 \mathrm{ng} / \mathrm{L}$ | $\mathrm{HPO}_{4}^{2-}$ | $<30 \mathrm{ng} / \mathrm{L}$ |
| $\mathrm{Ca}^{2+}$ | $45 \mathrm{ng} / \mathrm{L}$ | $\mathrm{SO}_{4}^{2-}$ | $128 \mathrm{ng} / \mathrm{L}$ |

Find the molar concentrations of $\mathrm{Na}^{+}$and $\mathrm{Cl}^{-}$in this water.
Use a prefix from Table 1-3 to express your answers.
S1-7. Find the molarity of pyridine $\left(\mathrm{C}_{5} \mathrm{H}_{5} \mathrm{~N}\right)$ if 5.00 g is dissolved in butanol to give a total volume of 457 mL .

S1-8. A $95.0 \mathrm{wt} \%$ solution of ethanol $\left(\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}\right.$, FM 46.07) in water has a density of $0.804 \mathrm{~g} / \mathrm{mL}$.
(a) Find the mass of 1.00 L of this solution and the number of grams of ethanol per liter.
(b) What is the molar concentration of ethanol in this solution?
(c) Find the molality of ethanol in this solution, considering $\mathrm{H}_{2} \mathrm{O}$ to be the solvent (even though $\mathrm{H}_{2} \mathrm{O}$ is really the solute in this case).

S1-9. (a) How many grams of the element nickel are contained in 10.0 g of a $10.2 \mathrm{wt} \%$ solution of nickel sulfate hexahydrate, $\mathrm{NiSO}_{4} \cdot 6 \mathrm{H}_{2} \mathrm{O}$ (FM 262.85)?
(b) The concentration of this solution is 0.412 M. Find the density.

S1-10. Describe how to prepare exactly 100 mL of 1.00 M HCl from 12.1 M HCl reagent.
S1-11. Describe how to prepare approximately 100 mL of $0.082 m \mathrm{NaClO}_{4}$ (FM 122.44).
S1-12. A $40.0 \mathrm{wt} \%$ solution of CsCl (FM 168.37) has a density of $1.43 \mathrm{~g} / \mathrm{mL}$, while a $20.0 \mathrm{wt} \%$ solution has a density of $1.18 \mathrm{~g} / \mathrm{mL}$.
(a) Find the molarity of CsCl in each solution.
(b) Find the molality of CsCl in each solution.
(c) How many mL of each solution should be diluted to 500 mL to make 0.100 M reagent? Why doesn't it take twice as much of the $20.0 \mathrm{wt} \%$ solution as the $40.0 \mathrm{wt} \%$ solution?

S1-13. How many grams and how many mL of $40.0 \mathrm{wt} \%$ urea solution (density $=1.111 \mathrm{~g} / \mathrm{mL}$ ) are required to react with 4.00 mmol of $\mathrm{Fe}^{3+}$ in the following reactions?

$$
\begin{aligned}
& \left(\mathrm{H}_{2} \mathrm{~N}\right)_{2} \mathrm{CO}+3 \mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{CO}_{2}+2 \mathrm{NH}_{4}^{+}+2 \mathrm{OH}^{-} \\
& \text {Urea } \\
& \mathrm{Fe}^{3+}+3 \mathrm{OH}^{-}+(x-1) \mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{FeOOH} \cdot x \mathrm{H}_{2} \mathrm{O}(s)
\end{aligned}
$$

S1-14. The constant $\hbar$ (read "h bar") is defined as $h / 2 \pi$, where $h$ is Planck's constant [6.626 $0755( \pm 0.0000040) \times 10^{-34} \mathrm{~J} \cdot \mathrm{~s}$ ]. Calculate the value and absolute uncertainty of $\hbar$. The number 2 is an integer (infinitely accurate) and $\pi$ is also an exact number. The first 10 digits of $\pi$ are 3.141592653 .

S2-1. Find the true mass of benzene $\left(\mathrm{C}_{6} \mathrm{H}_{6}\right.$, density $\left.=0.88 \mathrm{~g} / \mathrm{mL}\right)$ if the apparent mass in air is 9.947 g . Assume that the air density is $0.0012 \mathrm{~g} / \mathrm{mL}$ and the balance weight density is $8.0 \mathrm{~g} / \mathrm{mL}$.

S2-2. An aqueous solution prepared when the lab temperature was $19^{\circ} \mathrm{C}$ had a concentration 0.02764 M . What is the concentration of the same solution when used outdoors in the summer at $35^{\circ} \mathrm{C}$ ?

S2-3. Water from a $5-\mathrm{mL}$ pipet was drained into a weighing bottle whose empty mass was 9.974 g to give a new mass of 14.974 g at $26^{\circ} \mathrm{C}$. Find the volume of the pipet at $26^{\circ} \mathrm{C}$ and at $20^{\circ} \mathrm{C}$.

S3-1. Indicate how many significant figures there are in:
(a) 0.3050
(b) 0.003050
(c) $1.003 \times 10^{4}$

S3-2. Round each number as indicated:
(a) 5.1248 to 4 significant figures
(d) 0.1352371 to 4 significant figures
(b) 5.1244 to 4 significant figures
(e) 1.525 to 3 significant figures
(c) 5.1245 to 4 significant figures
(f) 1.525007 to 3 significant figures

S3-3. Write each answer with the correct number of digits:
(a) $3.021+8.99=12.011$
(d) $0.0302 \div\left(2.1143 \times 10^{-3}\right)=14.28369$
(b) $12.7-1.83=10.87$
(e) $\log \left(2.2 \times 10^{-18}\right)=$ ?
(g) $10^{-4.555}=$ ?
(c) $6.345 \times 2.2=13.9590$
(f) antilog $(-2.224)=$ ?

S3-4. Using the correct number of significant figures, find the formula mass of $\mathrm{C}_{6} \mathrm{H}_{13} \mathrm{~B}$.
S3-5. Find the absolute and percent relative uncertainty and express each answer with a reasonable number of significant figures.
(a) $3.4( \pm 0.2)+2.6( \pm 0.1)=$ ?
(c) $\left[3.4( \pm 0.2) \times 10^{-8}\right] \div\left[2.6( \pm 0.1) \times 10^{3}\right]=$ ?
(b) $3.4( \pm 0.2) \div 2.6( \pm 0.1)=$ ?
(d) $[3.4( \pm 0.2)-2.6( \pm 0.1)] \times 3.4( \pm 0.2)=$ ?

S3-6. Express the molecular mass ( $\pm$ uncertainty) of benzene, $\mathrm{C}_{6} \mathrm{H}_{6}$, with the correct number of significant figures.

S3-7. (a) A solution is prepared by dissolving $0.2222( \pm 0.0002) \mathrm{g}$ of $\mathrm{KIO}_{3}[\mathrm{FM} 214.0010$ $( \pm 0.0009)$ ] in $50.00( \pm 0.05) \mathrm{mL}$. Find the molarity and its uncertainty with an appropriate number of significant figures.
(b) Would the answer be affected significantly if the reagent were only $99.9 \%$ pure?

S3-8. Find the absolute and percent relative uncertainty and express each answer with a reasonable number of significant figures.
(a) $\sqrt{3.4( \pm 0.2)}=$ ?
(c) $10^{3.4}( \pm 0.2)=$ ?
(e) $\log [3.4( \pm 0.2)]=$ ?
(b) $[3.4( \pm 0.2)]^{2}=$ ?
(d) $\mathrm{e}^{3.4}( \pm 0.2)=$ ?
(f) $\ln [3.4( \pm 0.2)]=$ ?

S3-9. The value of Boltzmann's constant $(k)$ listed on the inside front cover of the book is calculated from the quotient $R / N$, where $R$ is the gas constant and $N$ is Avogadro's number. If the uncertainty in $R$ is $0.000070 \mathrm{~J} /(\mathrm{mol} \cdot \mathrm{K})$ and the uncertainty in $N$ is $0.0000036 \times 10^{23} / \mathrm{mol}$, find the uncertainty in $k$.

S3-10. Find the uncertainty in the molecular mass of $\mathrm{B}_{10} \mathrm{H}_{14}$ and write the molecular mass with the correct number of significant figures.

S4-1. Consider Rayleigh's data for the mass of gas from air in Table 4-3. Find the
(a) mean
(b) standard deviation
(c) variance

S4-2. Suppose that a Gaussian population of measurements has a mean of 1000 and a standard deviation of 50. What fraction of the population lies in the following intervals:
(a) $>1000$
(b) 950-1 050
(c) 850-1 150
(d) $<900$
(e) 930-1 030
(f) 912-991

S4-3. Write the equation of the smooth Gaussian curve in Figure 4-1. (Since the curve represents the results of 4768 measurements, and each bar on the graph corresponds to a $20-\mathrm{h}$ interval, you must use a factor of $4768 \times 20$ in the numerator of Equation 4-3.) Use the equation to calculate the value of $y$ when $x=1000 \mathrm{~h}$ and see if your calculated value agrees with the value on the graph.

S4-4. Find the 95 and $99 \%$ confidence intervals for the mean mass of nitrogen from chemical sources in Table 4-3.

S4-5. Two methods were used to measure the specific activity (units of enzyme activity per milligram of protein) of an enzyme. One unit of enzyme activity is defined as the amount of enzyme that catalyzes the formation of one micromole of product per minute under specified conditions.

Enzyme activity (five replications)

| Method 1: | 139 | 147 | 160 | 158 | 135 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Method 2: | 148 | 159 | 156 | 164 | 159 |

Is the mean value of method 1 significantly different from the mean value of method 2 at the $95 \%$ confidence level?

S4-6. It is known from many careful measurements that the concentration of magnesium in material is $0.137 \mathrm{wt} \%$. Your new analytical procedure gives values of $0.129,0.133,0.136,0.130,0.128$ and $0.131 \mathrm{wt} \%$. Do your results differ from the expected result at the $95 \%$ confidence level?

S4-7. Calcium in a mineral was analyzed five times by each of two methods, with similar standard deviations. Are the mean values significantly different at the $95 \%$ confidence level?

| Method 1: | 0.0271 | 0.0282 | 0.0279 | 0.0271 | 0.0275 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Method 2: | 0.0271 | 0.0268 | 0.0263 | 0.0274 | 0.0269 |

S4-8. The Ti content (wt \%) of two different ore samples was measured several times by the same method. Are the mean values significantly different at the $95 \%$ confidence level?

| Sample 1: | 0.0134 | 0.0138 | 0.0128 | 0.0133 | 0.0137 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Sample 2: | 0.0135 | 0.0142 | 0.0137 | 0.0141 | 0.0143 |

S4-9. The calcium content of a person's urine was determined on two different days:

| Day | Average $\mathrm{Ca}(\mathrm{mg} / \mathrm{L})$ | Number of measurements |
| :---: | :---: | :---: |
| 1 | 238 | 4 |
| 2 | 255 | 5 |

The analysis applied to many samples yields a standard deviation of $14 \mathrm{mg} / \mathrm{L}$. Are the two averages significantly different at the $95 \%$ confidence level?

S4-10. Using the $Q$ test, decide whether the value 0.195 should be rejected from the set of results: $0.217,0.224,0.195,0.221,0.221,0.223$.

S4-11. (a) The table below lists rainfall measured in Los Angeles. Enter this data into a spreadsheet and compute the average and standard deviation.
(b) Prepare a barchart showing rainfall as a function of year from 1878 to 1996.
(c) Prepare a histogram (another barchart) from this data showing rainfall in 2-inch intervals in the format below. For example, the bar at $x=15$ will show the number of years in which the rainfall was in the range 14.00 to 15.99 inches. In your judgement, does rainfall follow a Gaussian distribution?


| Year | Rainfall (inches) | Year | Rainfall (inches) | Year | Rainfall (inches) |
| ---: | :---: | ---: | :---: | ---: | :---: |
| 1878 | 20.860 | 1918 | 17.490 | 1958 | 17.490 |
| 1879 | 17.410 | 1919 | 8.820 | 1959 | 6.230 |
| 1880 | 18.650 | 1920 | 11.180 | 1960 | 9.570 |
| 1881 | 5.530 | 1921 | 19.850 | 1961 | 5.830 |
| 1882 | 10.740 | 1922 | 15.270 | 1962 | 15.370 |
| 1883 | 14.140 | 1923 | 6.250 | 1963 | 12.310 |
| 1884 | 40.290 | 1924 | 8.110 | 1964 | 7.980 |
| 1885 | 10.530 | 1925 | 8.940 | 1965 | 26.810 |
| 1886 | 16.720 | 1926 | 18.560 | 1966 | 12.910 |
| 1887 | 16.020 | 1927 | 18.630 | 1967 | 23.660 |
| 1888 | 20.820 | 1928 | 8.690 | 1968 | 7.580 |
| 1889 | 33.260 | 1929 | 8.320 | 1969 | 26.320 |
| 1890 | 12.690 | 1930 | 13.020 | 1970 | 16.540 |
| 1891 | 12.840 | 1931 | 18.930 | 1971 | 9.260 |
| 1892 | 18.720 | 1932 | 10.720 | 1972 | 6.540 |
| 1893 | 21.960 | 1933 | 18.760 | 1973 | 17.450 |
| 1894 | 7.510 | 1934 | 14.670 | 1974 | 16.690 |
| 1895 | 12.550 | 1935 | 14.490 | 1975 | 10.700 |
| 1896 | 11.800 | 1936 | 18.240 | 1976 | 11.010 |
| 1897 | 14.280 | 1937 | 17.970 | 1977 | 14.970 |
| 1898 | 4.830 | 1938 | 27.160 | 1978 | 30.570 |
| 1899 | 8.690 | 1939 | 12.060 | 1979 | 17.000 |
| 1900 | 11.300 | 1940 | 20.260 | 1980 | 26.330 |
| 1901 | 11.960 | 1941 | 31.280 | 1981 | 10.920 |
| 1902 | 13.120 | 1942 | 7.400 | 1982 | 14.410 |
| 1903 | 14.770 | 1943 | 22.570 | 1983 | 34.040 |
| 1904 | 11.880 | 1944 | 17.450 | 1984 | 8.900 |
| 1905 | 19.190 | 1945 | 12.780 | 1985 | 8.920 |
| 1906 | 21.460 | 1946 | 16.220 | 1986 | 18.000 |
| 1907 | 15.300 | 1947 | 4.130 | 1987 | 9.110 |
| 1908 | 13.740 | 1948 | 7.590 | 1988 | 11.570 |
| 1909 | 23.920 | 1989 | 1949 | 10.630 | 1989 |

S4-12. Students at Eastern Illinois University intended to prepare copper(II) carbonate by adding a solution of $\mathrm{CuSO}_{4} \cdot 5 \mathrm{H}_{2} \mathrm{O}$ to a solution of $\mathrm{Na}_{2} \mathrm{CO}_{3}$.

$$
\mathrm{CuSO}_{4} \cdot 5 \mathrm{H}_{2} \mathrm{O}(a q)+\mathrm{Na}_{2} \mathrm{CO}_{3}(a q) \rightarrow \underset{\text { copper(II) carbonate }}{\mathrm{CuCO}_{3}(s)+\mathrm{Na}_{2} \mathrm{SO}_{4}(a q)+5 \mathrm{H}_{2} \mathrm{O}(l)}
$$

After warming the mixture to $60^{\circ} \mathrm{C}$, the gelatinous blue precipitate coagulated into an easily filterable pale green solid. The product was filtered, washed, and dried at $70^{\circ} \mathrm{C}$. Copper in the product was measured by heating 0.4 g of solid in a stream of methane at high temperature to reduce the solid to pure Cu , which was weighed.

$$
4 \mathrm{CuCO}_{3}(s)+\mathrm{CH}_{4}(g) \stackrel{\text { heat }}{\rightarrow} 4 \mathrm{Cu}(s)+5 \mathrm{CO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(g)
$$

In 1995, 43 students found a mean value of $55.6 \mathrm{wt} \% \mathrm{Cu}$ with a standard deviation of 2.7 $\mathrm{wt} \%$. In 1996, 39 students found $55.9 \mathrm{wt} \%$ with a standard deviation of $3.8 \mathrm{wt} \%$. The instructor tried the experiment 9 times and measured $55.8 \mathrm{wt} \%$ with a standard deviation of $0.5 \mathrm{wt} \%$. Was the product of the reaction probably $\mathrm{CuCO}_{3}$ ? Could it have been a hydrate, $\mathrm{CuCO}_{3} \cdot x \mathrm{H}_{2} \mathrm{O}$ ? [This problem was taken from D. Sheeran, J. Chem. Ed. 1998, 75, 453. See also H. Gamsjäger and W. Preis, J. Chem. Ed. 1999, 76, 1339.]

