Sultan Qaboos University-College of Science Department of Mathematics and Statistics MATH 3171 - Linear Algebra & Multivariate Calculus for Engineers Spring Semester 2008 - QUIZ # 3-A

Date: 7 April 2008 NAME:

- 1. [4 marks] Find the projection (component) of the vector a = [-2, 3, -1] in the direction of b = [4, -2, 0].
- 2. [5 marks] Is the following statement true or false? Explain your answer. For all vectors $u(t) = [u_1(t), u_2(t), u_3(t)]$ and $v(t) = [v_1(t), v_2(t), v_3(t)]$, $\frac{d}{dt}(u(t) \cdot v(t)) = \frac{d}{dt}u(t) \cdot \frac{d}{dt}v(t)$
- 3. [6 marks] Find the area of the parallelogram if the vertices are (1,1,1), (4,4,4), (8,-3,14) and (11,0,17).

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- 1. [6 marks] Find the angles of the parallelogram if the vertices are (1,2,3), (3,5,7), (2,0,9) and (4,3,13).
- 2. [5 marks] Give an example of a vector u(t) = [f(t), g(t), h(t)] such that not all f(t), g(t), h(t) are constants but |u(t)| is constant. What is the relationship between u(t) and $\frac{d}{dt}u(t)$? Explain your answer.
- 3. [4 marks] Find $\frac{\partial v}{\partial x}$, $\frac{\partial v}{\partial y}$ and $\frac{\partial^2 v}{\partial y \partial z}$ if $v(x, y, z) = [\cos x \cosh y, -\sin x \sinh y, \ln(yz)].$

Sultan Qaboos University-College of Science Department of Mathematics and Statistics MATH 3171 - Linear Algebra & Multivariate Calculus for Engineers Spring Semester 2008 - QUIZ # 3-C

Date: 7 April 2008 NAME:

- 1. [5 marks] Show that for any two vectors u and v, $|u + v| \le |u| + |v|$.
- 2. [6 marks] Find the volume of the Tetrahedron if the vertices are (1,1,1), (5,-7,3), (7,4,8) and (10,7,4).
- 3. [4 marks] Find $\frac{\partial^2 v}{\partial x^2}$ and $\frac{\partial^2 v}{\partial x \partial y}$ if $v(x, y, z) = \cos(xyz)(\mathbf{i} + \mathbf{j})$.

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Date: 7 April 2008 NAME:

- 1. [4 marks] Is the following statement true or fallse? Explain your answer. For all vectors u, v and w with $u \neq 0$, if $u \cdot v = u \cdot w$ then v = w.
- 2. [6 marks] Find two unit normal vectors to the plane through the points (1,3,0), (2,0,8), (0,2,2) and then find the equation of the plane.
- 3. [5 marks] Find $\frac{\partial v}{\partial x}, \frac{\partial v}{\partial y}$ and $\frac{\partial^2 v}{\partial x \partial z}$ if $v(x, y, z) = \left[\frac{1}{2}\ln(x^2 + y^2), \tan^{-1}(\frac{y}{x}), \frac{-z}{e}\right]$.